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New analysis concerning the strange quark polarization puzzle

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OUTLINE

- The **strange** quark polarization **puzzle**

→ conflict between $\Delta s(x)_{\text{DIS}}$ and $\Delta s(x)_{\text{DIS+SIDIS}}$ if *de Florian, Sassot, Stratmann* (DSS) fragmentation functions (FFs) are used

- A new **NLO QCD** analysis of the world **polarized inclusive** DIS data including for the first time the new **extremely precise CLAS** data is presented

→ A more general input parametrization for $\Delta s(x)$ which allows for a **change sign** of the strange quark density is used

→ The results **confirm** that the polarized **inclusive** DIS data yield **significantly negative** values for the polarized strange quark density

- **Summary**

Polarized **inclusive** DIS processes

Due to the **lack** of the charged current **neutrino** data *only* the sums

$$(\Delta q + \Delta \bar{q})(x, Q^2)$$

can be determined from the polarized **inclusive** DIS data !

$$g_1(x, Q^2)_{LT} = \frac{1}{2} \sum_q^{N_f} e_q^2 [(\Delta q + \Delta \bar{q}) \otimes (1 + \frac{\alpha_s(Q^2)}{2\pi} \delta C_q) + \frac{\alpha_s(Q^2)}{2\pi} \Delta G \otimes \frac{\delta C_G}{N_f}]$$

LT – leading twist **NLO QCD** contribution

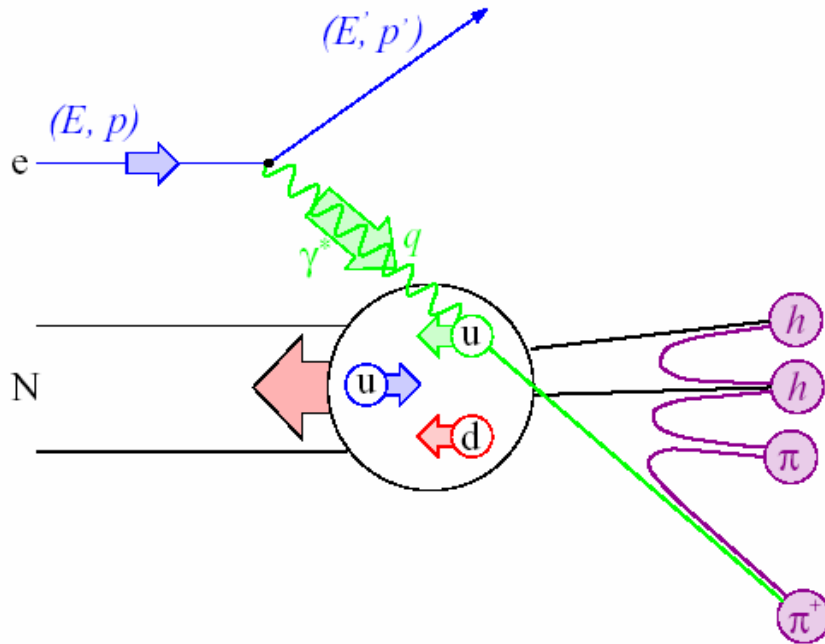
$\delta C_q, \delta C_G$ – *Wilson* coefficient functions

- It is **important** that in contrast to the light sea quark densities $\Delta \bar{u}$ and $\Delta \bar{d}$, $(\Delta s + \Delta \bar{s})$ can be **well** determined **only** from the inclusive **DIS** experiments, if the data are sufficiently precise.

Semi-inclusive processes

→ allow to separate Δq and $\Delta \bar{q}$

Fragmentation functions – new quantities



D_q^h from quark q into hadron h
 $z = \frac{E_h}{\nu}$ energy fraction carried by h

$$A_1^h(x, z, Q^2) = \frac{g_1^h - \gamma^2 g_2^h}{F_1^h}$$

In LO QCD

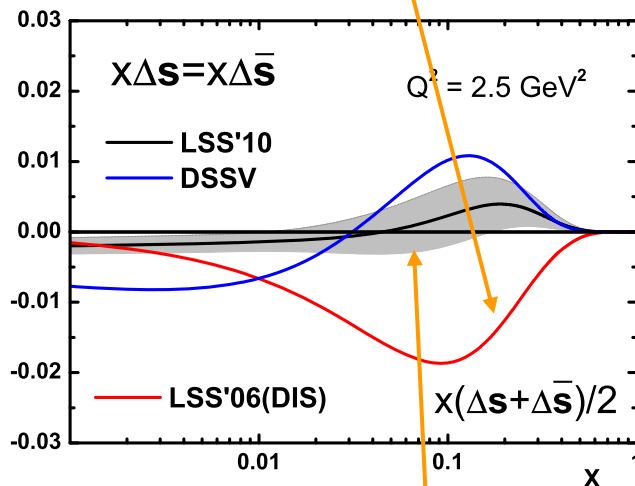
$$A_1^h(x, z, Q^2) \sim \frac{g_1^h}{F_1^h} = \frac{\sum_f e_f^2 \Delta q_f(x, Q^2) \mathbf{D}_f^h(z, Q^2)}{\sum_f e_f^2 q_f(x, Q^2) \mathbf{D}_f^h(z, Q^2)}$$

In NLO QCD the Wilson coefficients $\Delta C_{ij}(x, z)$ have to be included

The status of the strange quark polarization puzzle before this analysis

- $\Delta s(x) = \Delta \bar{s}(x)$ **negative** from **all** analyses of the **inclusive DIS** data !!!

→ **Disadvantage:** in all of them simple input parametrizations for the **polarized** strange quark density, which **do not permit a sign change** of the density, have been used (it was impossible to determine from the DIS data available at that time the parameter corresponding to the sign change).



Although their **first moments** are **negative** and almost equal, $\Delta s(x)$ (**DIS**) and $\Delta s(x)$ (**DIS+SIDIS**) are **quite different**

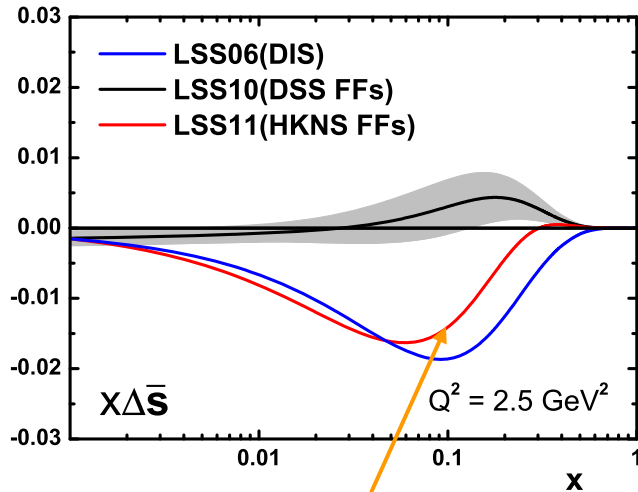
- The **very small** values of the strange quark density obtained from combined analyses of DIS and **SIDIS** data using the **DSS FFs** are **in contradiction** with **significantly negative** values of this quantity obtained from **inclusive DIS** data.

→ In the **SIDIS** analyses the results on $\Delta s(x)$ **strongly** depend on the **kaon FFs** used which are still **not** reliably determined.

Impact of the kaon FFs on polarized strange quark density

$$\Delta s(x) = \Delta \bar{s}(x)$$

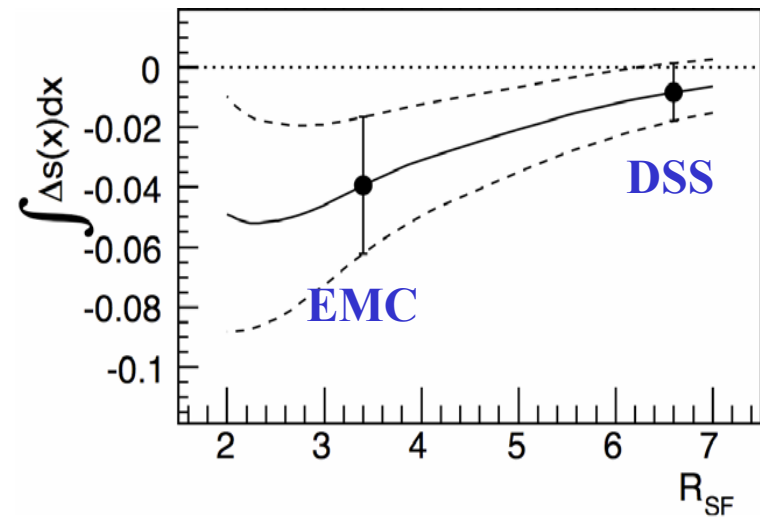
LSS: PR D84 (2011) 014002



LSS results for $\Delta s(x)$ from **NLO QCD** analyses of **DIS+SIDIS** polarized data using 2 sets of FFs (**DSS** and **HKNS**).

Note that $\Delta s(x)$ extracted using the kaon **HKNS** FFs is **negative** and very close to that obtained from the **inclusive DIS** data.

PLB 693 (2010) 227-235



COMPASS LO results for Δs integrated over x using measured spin asymmetries for **SIDIS** and 2 sets of FFs (**DSS** and **EMC**).

$$R_{SF} \equiv \frac{\int D_s^{K^+}(z, Q^2) dz}{\int D_u^{K^+}(z, Q^2) dz}$$

- Keeping in mind that **the present** sets of **kaon** FFs are **NOT consistent** with the recently published *HERMES* and the preliminary *COMPASS* data on the hadron multiplicities, *one can conclude* now that the values of the polarized strange quark density $\Delta s(x)$ determined from the analyses in the presence of SIDIS data, **cannot** be correct.

NB: Note also that in the extraction of the **NLO DSS** set of FFs there was a **mistake** for the longitudinal Wilson coefficient $C_{qg}^L(x, z)$ in the theoretical expression for the multiplicities.

- **New** sets of **pion NLO** FFs were extracted by **LSS** from the HERMES data on multiplicities (*arXiv:1312.5200*) and by **DSEHS (DSS+)** from a global fit to $e^+e^- \oplus SI$ pp (RICH) \oplus HERMES data (*PR D91 (2015) 014035*).

NB: The version of the **DSS+** analysis presented at HEP (*arxiv:1410.6027*) is **wrong** and **NOT** yet updated !?

- A **reliable** determination of **kaon FFs** (in progress) is **badly** needed in order to extract **correctly** the **polarized strange quark density** from the polarized **SIDIS** processes !
- In what follows we present our results of a **NLO** QCD analysis of the **polarized inclusive** DIS data including in the world data set for the first time the recent **very precise JLAB CLAS data** on the proton and deuteron **spin** structure functions.

The aim of the analysis is to answer the question, if it is possible to determine the **polarized strange quark density** using a more general input parametrization which allows for a **sign change** of the density in Bjorken x .

Remark !

- An important difference between the kinematic regions of the unpolarized and *polarized* data sets
- A **half** of the present **inclusive** data are at **moderate** Q^2 and W^2 :

$$Q^2 \approx 1 - 4 \text{ GeV}^2, \quad 4 < W^2 < 10 \text{ GeV}^2$$

*preasymptotic
region*

$$g_1(x, Q^2) = g_1(x, Q^2)_{\text{LT/NLO}} + \frac{M^2}{Q^2} h^{\text{TMC}}(x, Q^2) + \frac{h^{\text{HT}}(x, Q^2)}{Q^2} + O(1/Q^4)$$

→ The **higher twist (HT)** corrections to g_1 are **NOT** negligible in the **preasymptotic** region and have to be accounted for

NLO QCD fit to world polarized inclusive DIS data

$$\left[\begin{array}{c} g_1 \\ F_1 \end{array} \right]_{\text{exp}} \stackrel{\chi^2}{\Leftrightarrow} \frac{(g_1)_{\text{NLO}} + (g_1)_{\text{TMC+HT}}}{(F_1)_{\text{exp}}}$$

$$g_1(x, Q^2)_{\text{NLO}} = \frac{1}{2} \sum_q^{N_f} e_q^2 [(\Delta q + \Delta \bar{q}) \otimes (1 + \frac{\alpha_s(Q^2)}{2\pi} \delta C_q) + \frac{\alpha_s(Q^2)}{2\pi} \Delta G \otimes \frac{\delta C_G}{N_f}]$$

$$(g_1)_{\text{TMC+HT}}(x, Q^2) = \frac{M^2}{Q^2} h^{\text{TMC}}(x, Q^2) + \frac{h^{\text{HT}}(x, Q^2)}{Q^2}$$

$$2xF_1(x, Q^2)_{\text{exp}} = F_2(x, Q^2)_{\text{exp}} (1 + \gamma^2) / (1 + R(x, Q^2)_{\text{exp}}), \quad \gamma^2 = 4M^2 x^2 / Q^2$$

$F_{2\text{exp}}$ – NMC parametrization of F_2 data, R_{exp} – SLAC parametrization of R data

Input parametrization for the polarized PDFs at $Q^2 = 1 \text{ GeV}^2$:

$$x(\Delta u + \Delta \bar{u})(x) = N_u x^{\alpha_u} (1-x)^{\beta_u} (1 + \varepsilon_u \sqrt{x} + \gamma_u x)$$


$$x(\Delta d + \Delta \bar{d})(x) = N_d x^{\alpha_d} (1-x)^{\beta_d} (1 + \gamma_d x)$$

$$x(\Delta s + \Delta \bar{s})(x) = N_s x^{\alpha_s} (1-x)^{\beta_s} (1 + \gamma_s x) !$$

$$x\Delta G(x) = N_g x^{\alpha_g} (1-x)^{\beta_g} (1 + \gamma_g)$$

$\beta_s = \beta_g = \beta_{sea}(MRST'02)$ – to guarantee **positivity** constraints

Sum rules from hyperon β -decays


$$a_3 = g_A = (\Delta u + \Delta \bar{u})(Q^2) - (\Delta d + \Delta \bar{d})(Q^2) = F - D = 1.269 \pm 0.003$$

$$a_8 = (\Delta u + \Delta \bar{u})(Q^2) + (\Delta d + \Delta \bar{d})(Q^2) - 2(\Delta s + \Delta \bar{s})(Q^2) = 3F - D = 0.585 \pm 0.025$$

$15 - 2(\text{SR}) = 13$ free parameters

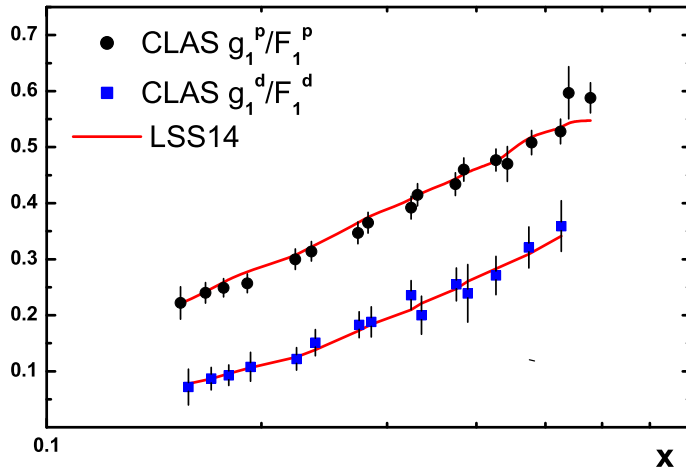
SU(3) symmetric value

NB. Contrary to the previous analyses, additional assumptions about the **sea** quark densities $\Delta \bar{q}(x)$ are **not** made.

A good description of the data is achieved

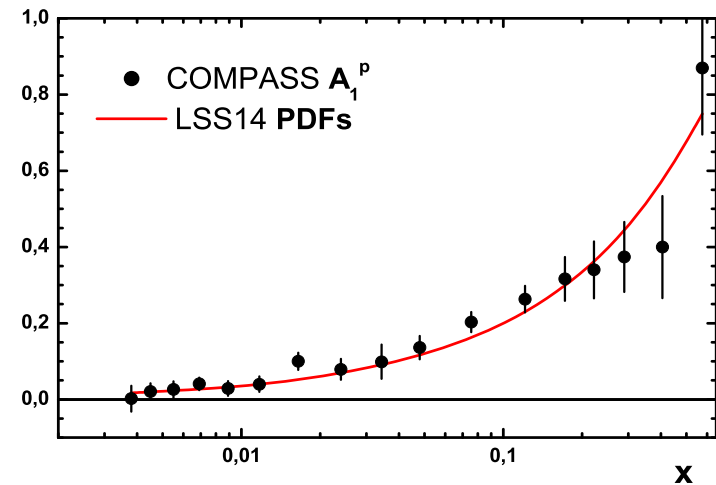
$$\chi^2 / DOF = 0.842 \text{ for } 902 \text{ exp. points}$$

The statistical and systematic errors are taken in quadrature



For CLAS p data: $\chi^2 / Nrp = 0.55$

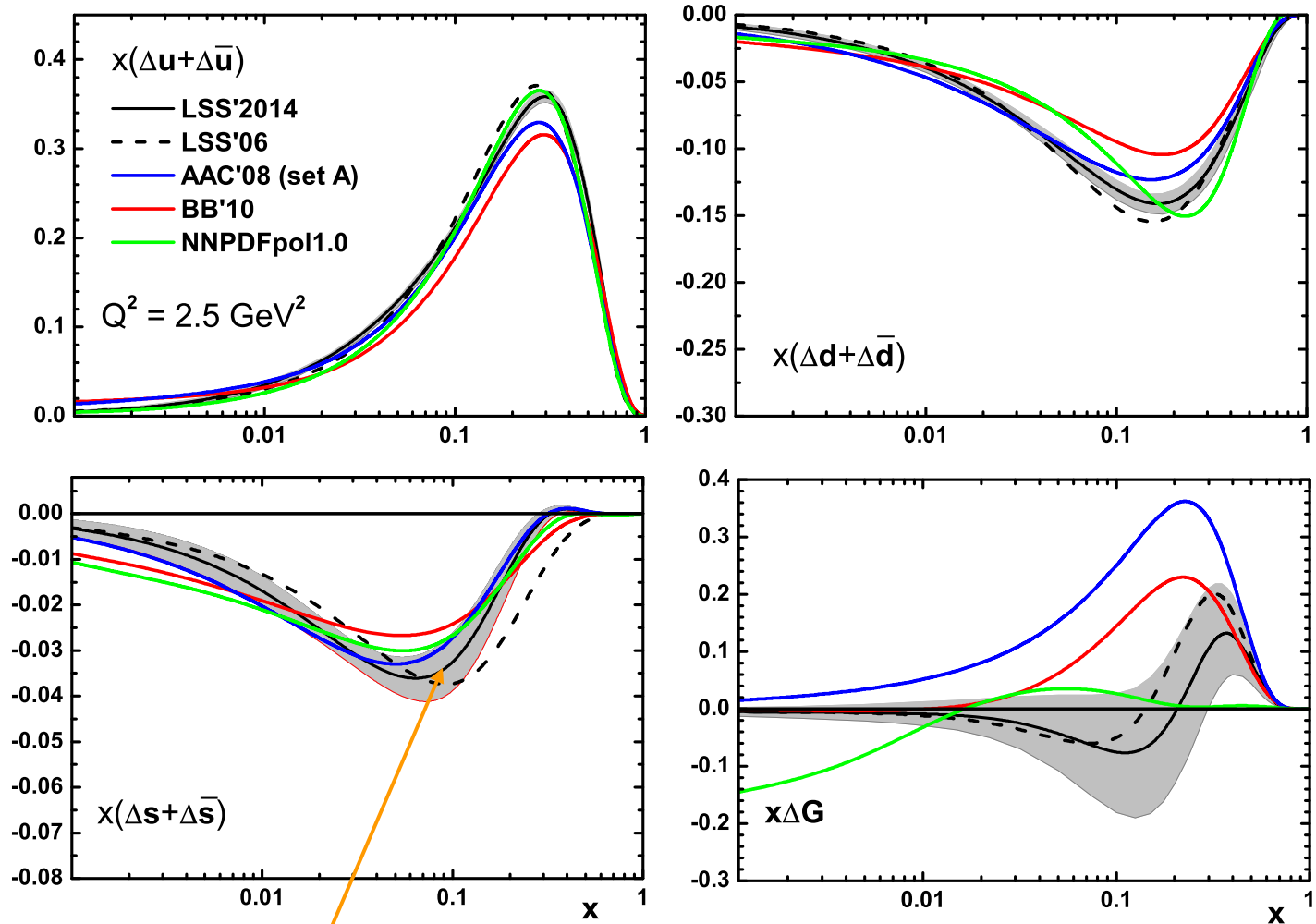
For CLAS d data: $\chi^2 / Nrp = 0.23$



Comparison between the new COMPASS A_1^p data which were presented after our fit was made and the asymmetry calculated at the measured points using the LSS'14 PDFs.

→ A very good description: $\chi^2 / Nrp = 0.68$

Extracted NLO polarized PDFs – LSS'14



- ! The extracted **strange quark density** remains **significantly negative** even though the parametrization allowed a sign change as a function of x .

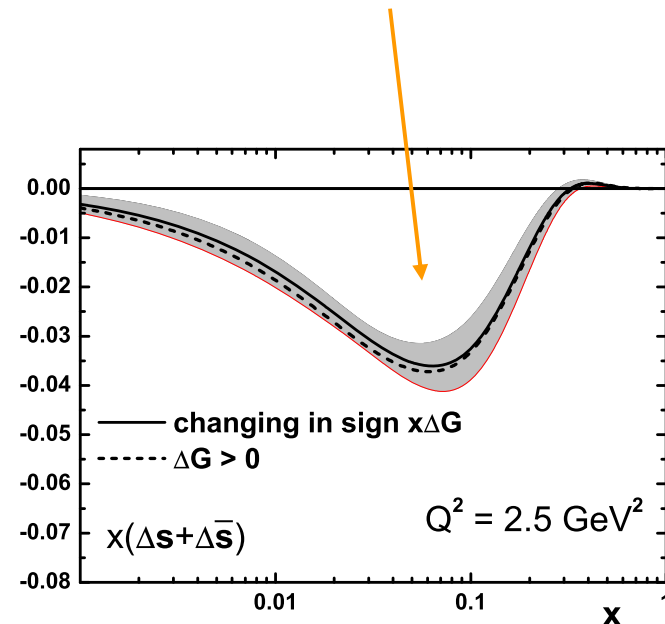
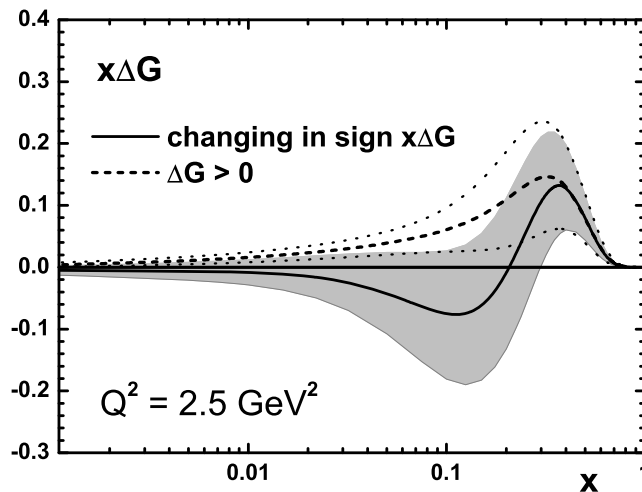
$$(\Delta s + \Delta \bar{s})(Q^2) = -0.106 \pm 0.023 \text{ at } Q^2 = 1 \text{ GeV}^2$$

We have found that the present polarized inclusive DIS data still cannot rule out the solution with a **positive** gluon polarization.

$$\chi^2 / DOF(\text{node } x\Delta G) = 0.842 \text{ and } \chi^2 / DOF(x\Delta G > 0) = 0.845$$

and the data **cannot** distinguish between these two solutions.

The polarized strange sea quark densities obtained in the fits with sign-changing or positive gluons are **almost identical**



Sensitivity of the polarized strange quark density to flavor SU(3) symmetry breaking

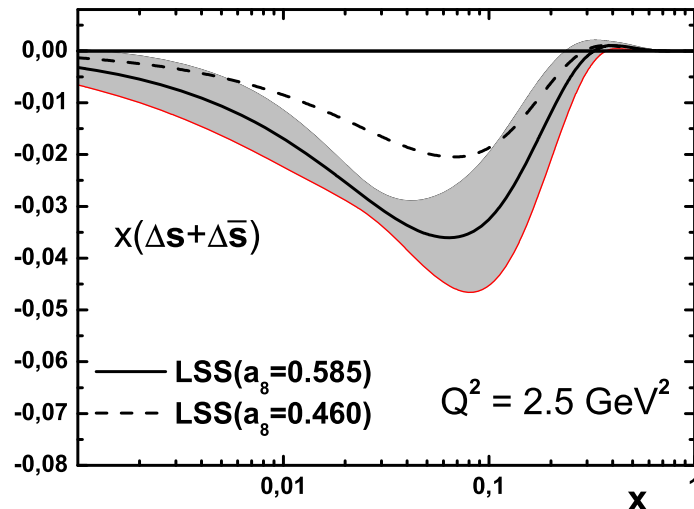
If **SU(3) symmetry** of the hyperon β – decays **holds**

$$\rightarrow a_8 = (\Delta u + \Delta \bar{u})(Q^2) + (\Delta d + \Delta \bar{d})(Q^2) - 2(\Delta s + \Delta \bar{s})(Q^2) = 3F - D = 0.585 \pm 0.025$$

The question about the SU(3) symmetry breaking is **still open**.

There are different theoretical models. Here we present the result on the strange quark density, if instead of the SU(3) symmetric value of a_8 , the value **0.46** is used. This value corresponds to the **maximal reduction** of a_8 (**20%**) presented in the literature (*S. Bass, A.W. Thomas, PL B684 (2010)*).

The **key point** is that the **shape** of the polarized strange quark density **is the same**.



SUMMARY

- A new **NLO QCD** analysis of the world **polarized inclusive DIS** data, including for the first time the new **extremely precise CLAS** data on the proton and deuteron **spin** str. functions, is presented
- Despite allowing in the parametrization of $(\Delta s + \Delta \bar{s})(x)$, for a **possible sign change**, we have **confirmed** the previous claim, namely, that the **inclusive** data yield **significantly negative** values for the **polarized strange quark density**.

We believe that the present **disagreement** between the SIDIS and DIS strange quark polarizations very likely results from a **lack of correct information for the kaon fragmentation functions** utilized and that the results from the inclusive analysis are correct.